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*Roger Prud'homme*

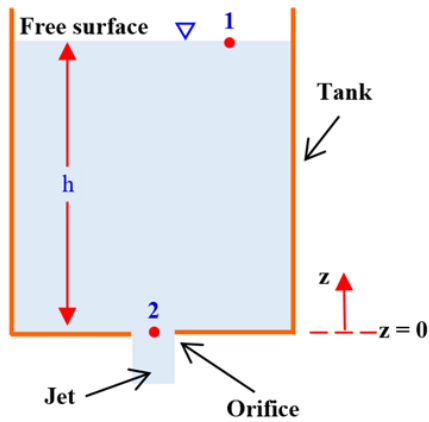
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# **Dimensional Analysis and Similarity in Fluid Mechanics**

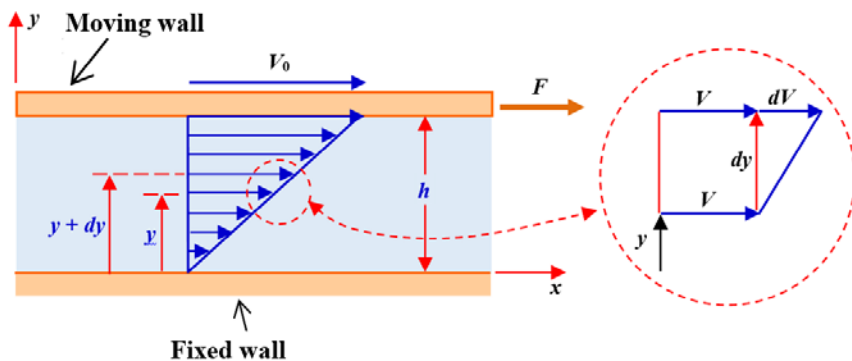
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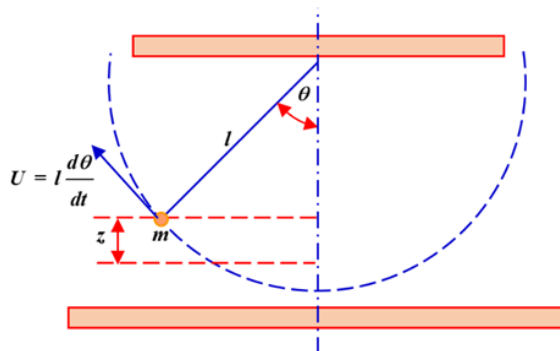
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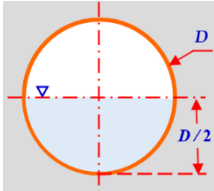
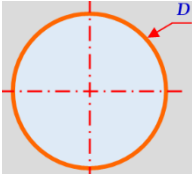
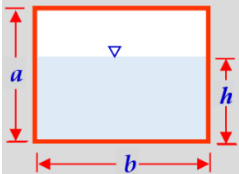
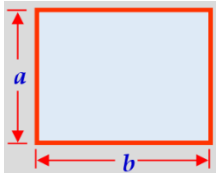
**Figure 1.1.** Flow through an orifice, establishing of the Torricelli relationship;  
HRP: horizontal reference plane



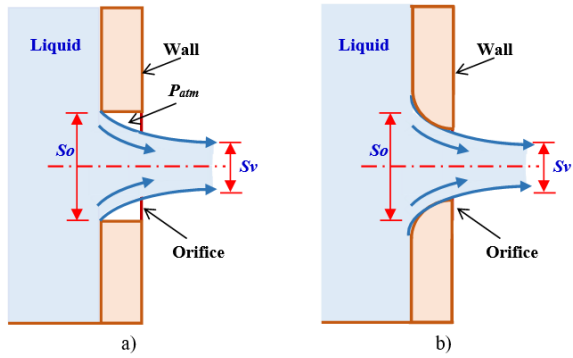
**Figure 1.2.** Newton's experiment known as the "moving wall"



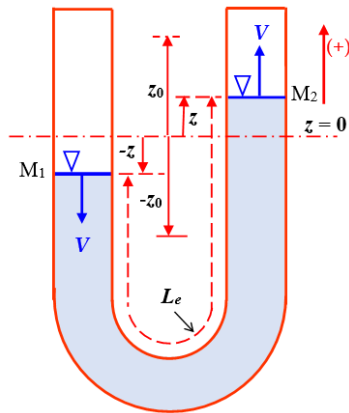
**Figure 2.1.** Pendulum in oscillation:  $z = l(1 - \cos\theta)$ .

	Free surface flow	Load flows
Shape of cross section		
Cross-section area	$S_m = \frac{1}{2} \frac{\pi D^2}{4}$	$S_m = \frac{\pi D^2}{4}$
Wetted perimeter	$Pe_m = \frac{\pi D}{2}$	$Pe_m = \pi D$
Hydraulic diameter	$D_H = \frac{4S_m}{Pe_m} = D$	$D_H = \frac{4S_m}{Pe_m} = D$
Shape of cross section		
Cross-section area	$S_m = bh$	$S_m = ab$
Wetted perimeter	$Pe_m = b + 2h$	$Pe_m = 2(b + a)$
Hydraulic diameter	$D_H = \frac{4bh}{b + 2h}$	$D_H = \frac{4bh}{2(a + b)}$

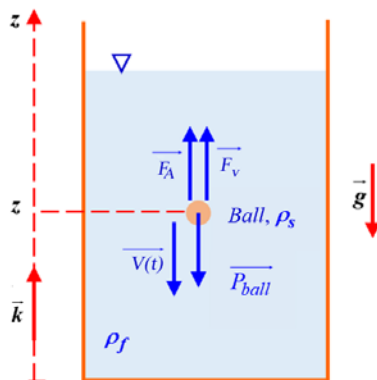
**Table 2.1.** Some expressions of hydraulic cross-section diameter using simple geometry



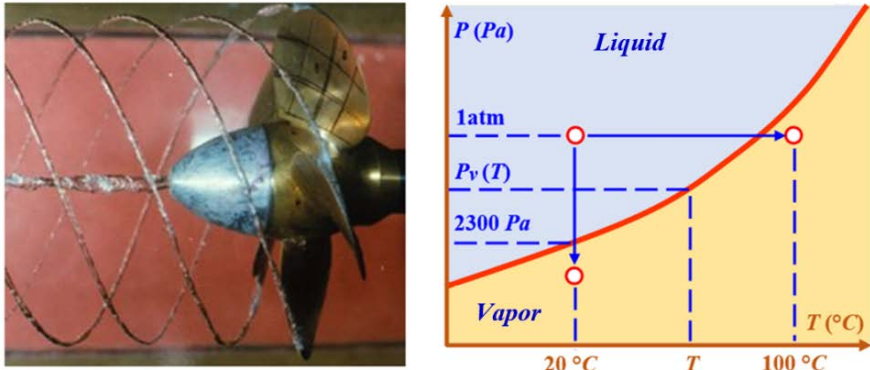
**Figure 2.4.** Flow through orifices: (a) a thin-walled orifice; (b) a round-edged orifice



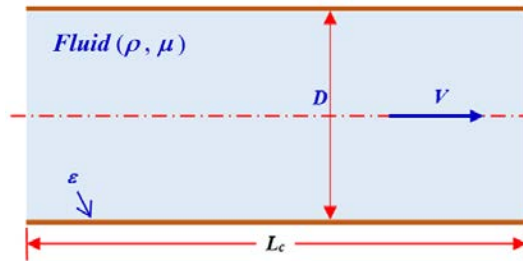
**Figure 2.6.** Oscillation of a liquid in a U-shaped tube



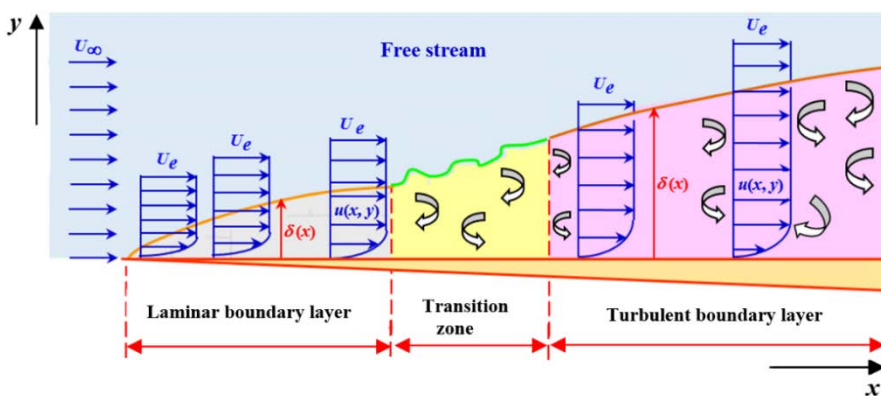
**Figure 2.7.** Falling ball viscometer



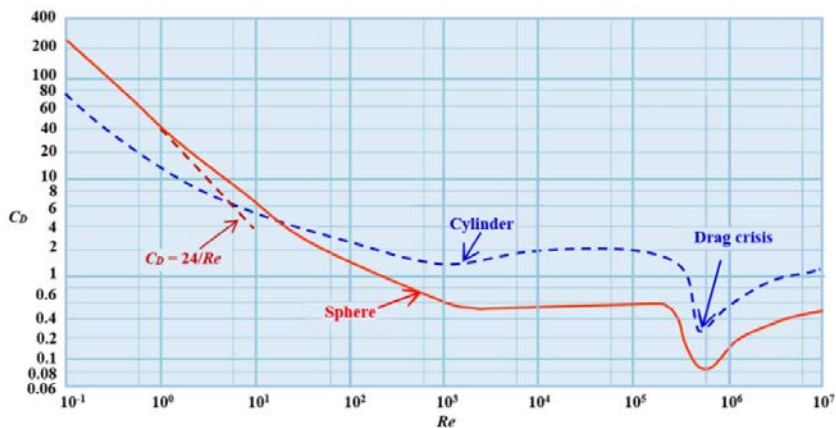
**Figure 2.8.** The phenomenon of cavitation and its thermodynamic diagram:  
a) an example of cavitation occurring on a propeller; b) thermodynamic diagram

















**Figure 2.9.** Pressure drop in horizontal pipe of circular cross-section



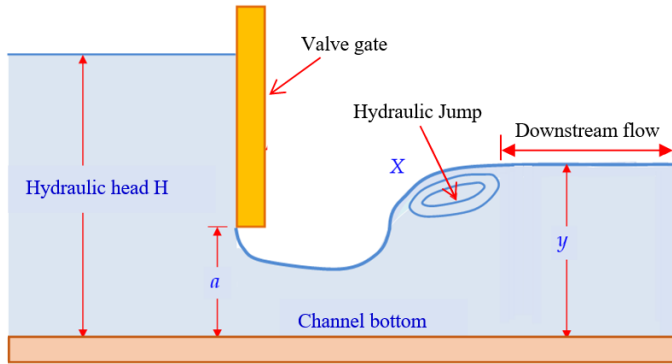
**Figure 2.10.** Flow near a flat wall (dynamic boundary layers)



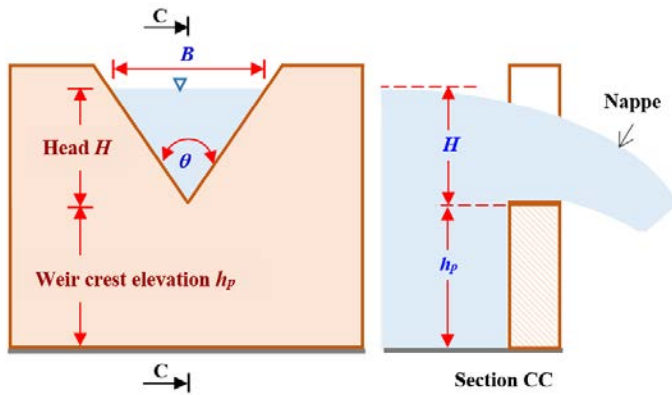
**Figure 2.11.** Variation of the drag coefficient as a function of the Reynolds number in the case of a sphere and a cylinder

	Shape	$C_D$		Shape	$C_D$
Two dimensional	Square			Half tube	
		2.1			1.2
		1.6			2.3
	Half cylinder			Equilateral triangle	
		1.2			1.6
		1.7			2.0
Three dimensional	Cub			Spherical cap	
		1.07			0.4
		0.81			1.4
	Cone	$\theta$ (°)	$C_D$	Parachute	
		10	0.30		1.2
		20	0.40		
		30	0.55		
		40	0.65		
		60	0.80		
		90	1.15		

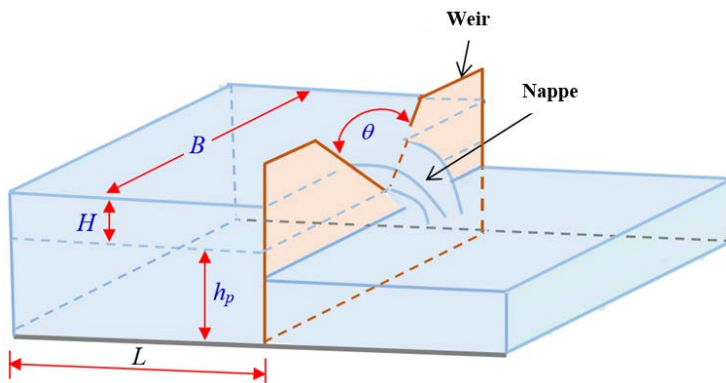
**Table 2.5.** Drag coefficient values for two-dimensional and three-dimensional objects calculated on the front surface area for a Reynolds number greater than or equal to  $10^5$



**Figure 2.12.** *Flow in a channel*



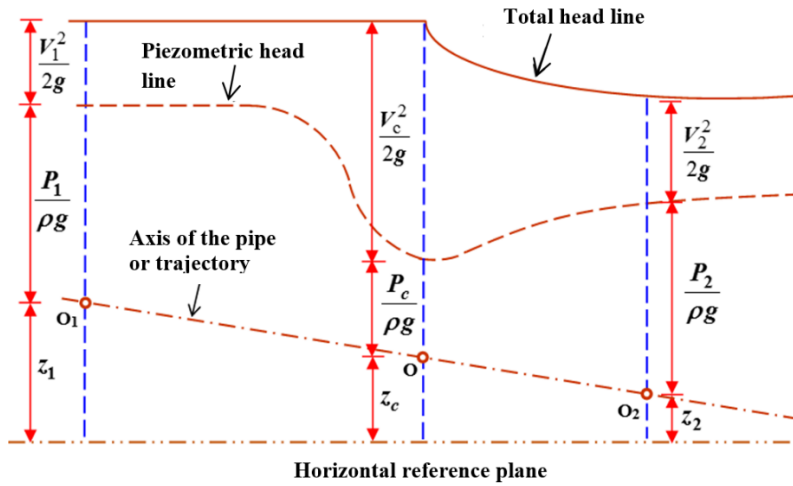
**Figure 2.13.** *Dimensions of a triangular spillway*



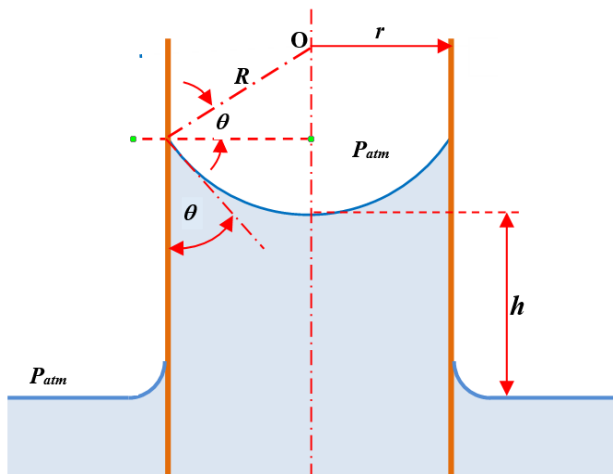
**Figure 2.14.** *Triangular notch weir with thin wall, placed in a hydraulic channel*



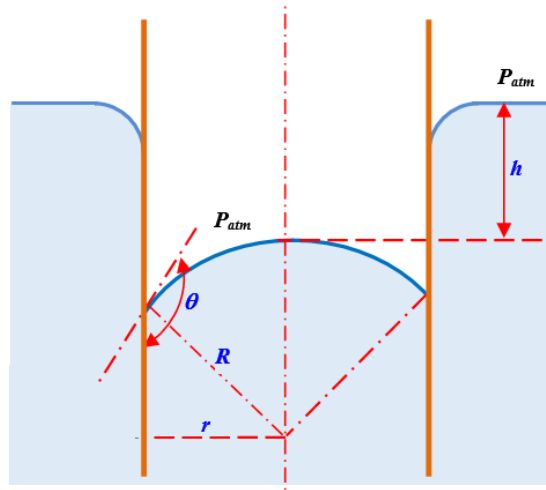




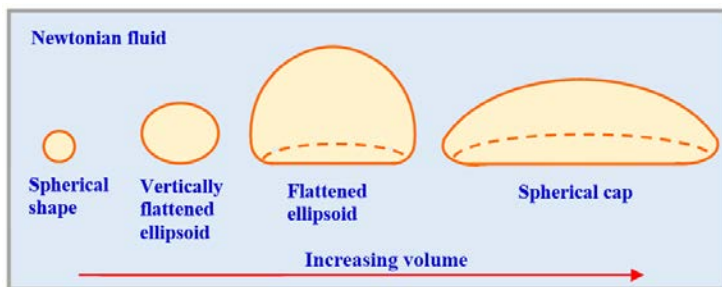
**Figure 2.17.** Progression of the load line and the piezometric line through a sharply narrowing segment



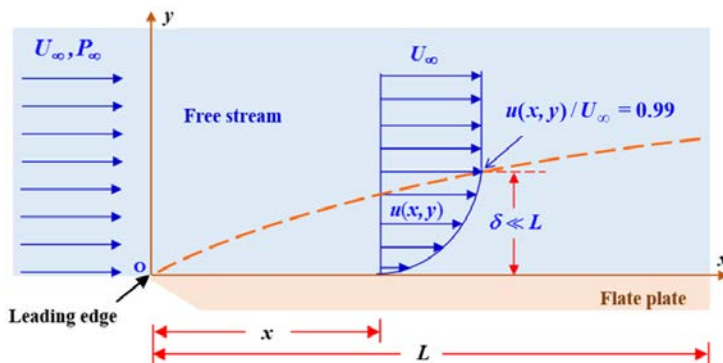
**Figure 2.18.** Capillary rise in the case of water that dampens the solid from which the capillary tube is created



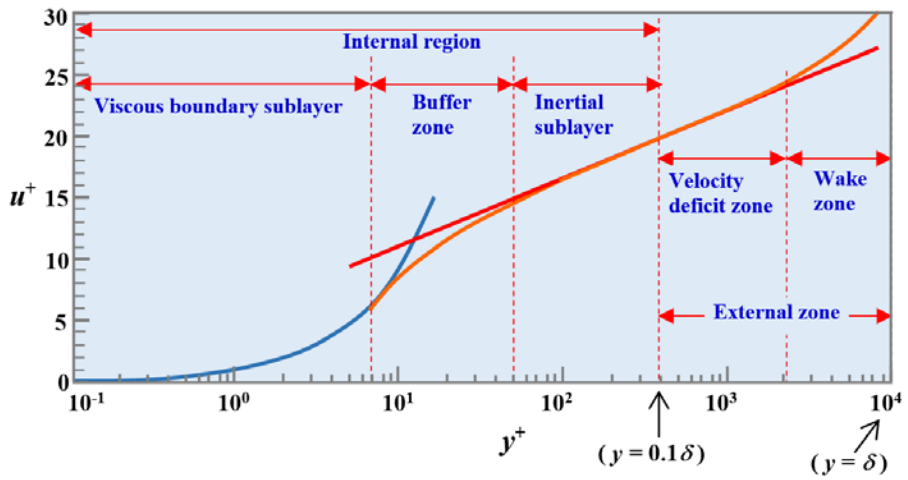
**Figure 2.19.** Capillary depression in the case of mercury that does not dampen the solid from which the capillary tube is made



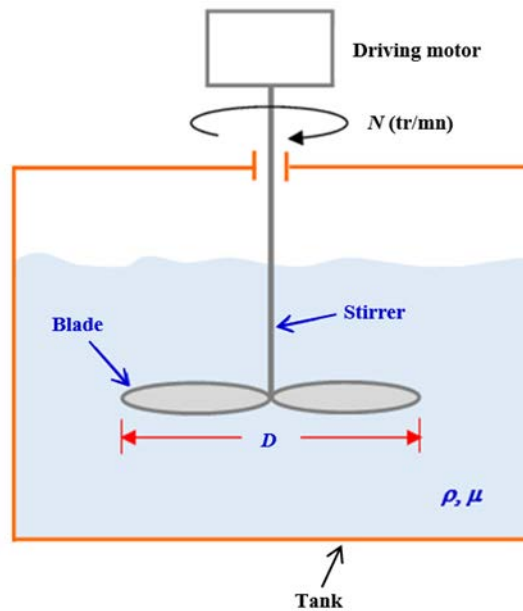
**Figure 2.20.** Generic form of bubbles in a Newtonian fluid



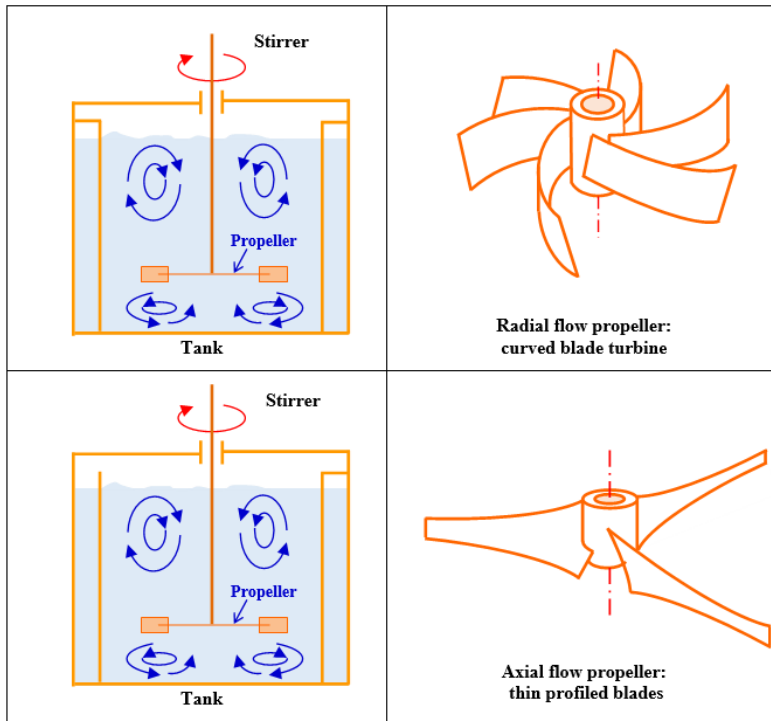
**Figure 2.21.** Laminar dynamic boundary layer on a flat wall



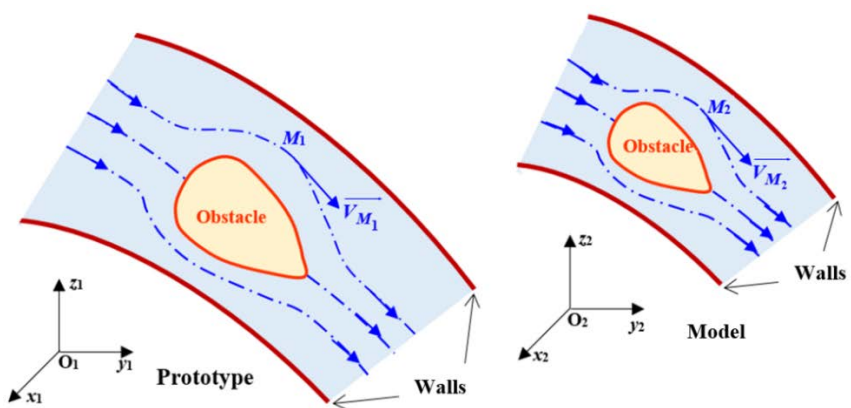
**Figure 2.22.** Velocity profile through the turbulent boundary layer of a flat plate



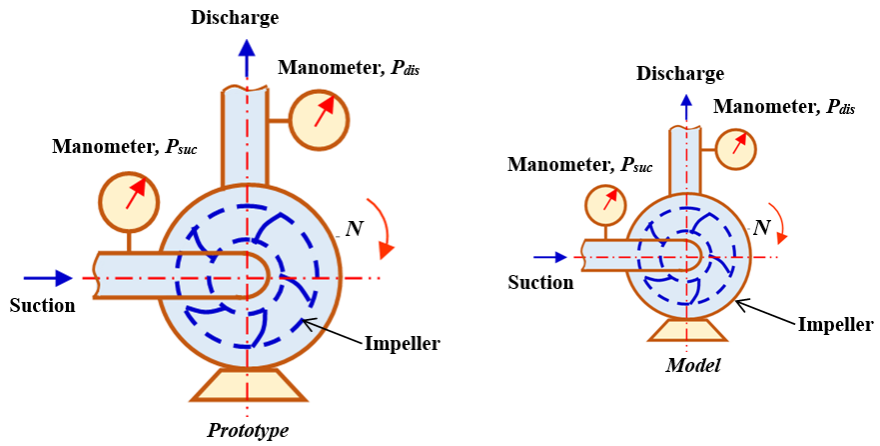
**Figure 2.23.** Scheme of a stirrer for liquids



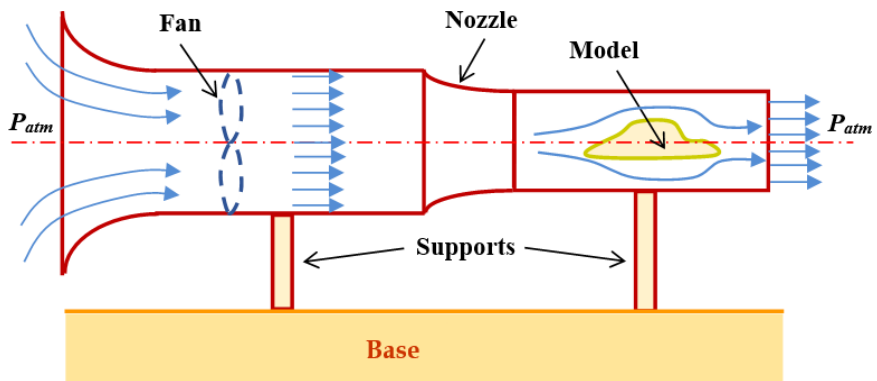
**Figure 2.24.** Example of axial and radial flow propellers



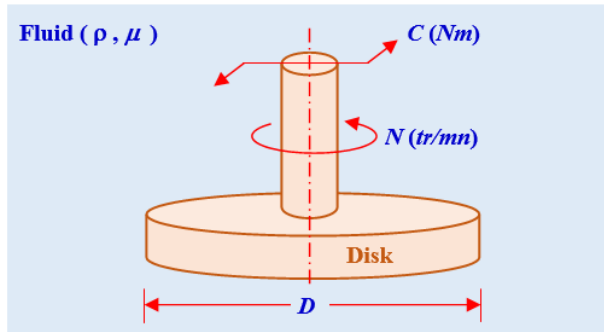
**Figure 3.1.** Similarity of two flows



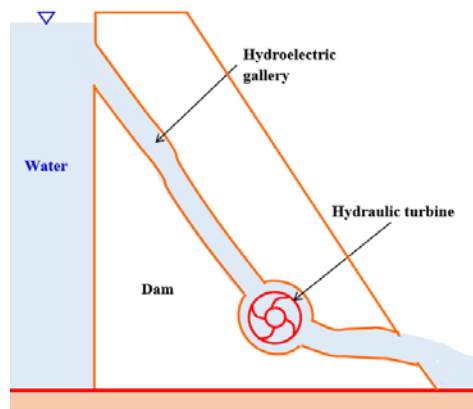
**Figure 3.2.** *Model and prototype of a centrifugal pump*



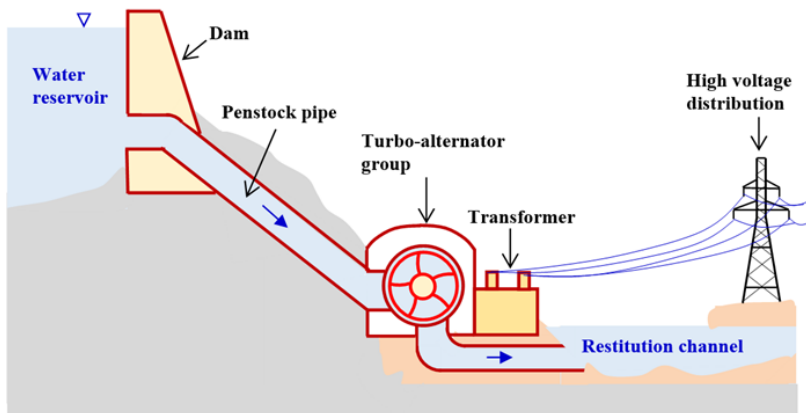
**Figure 3.3.** *Diagram of a wind tunnel*



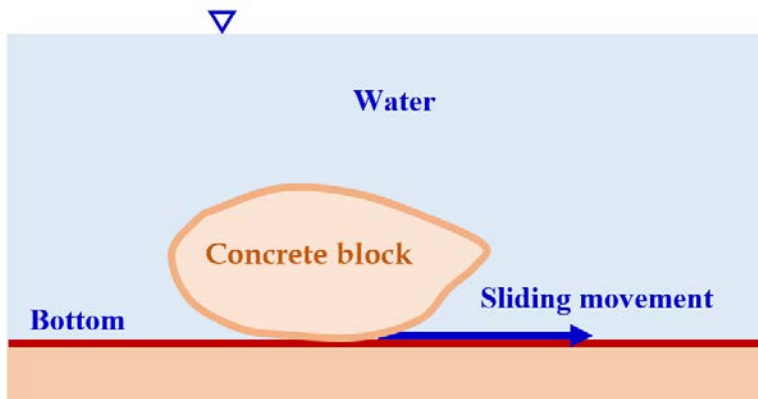
**Figure 3.4.** *Disk rotating in a viscous fluid*



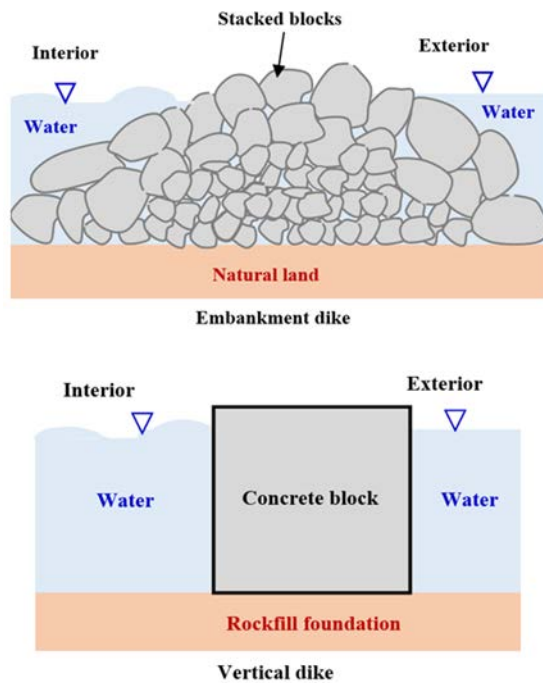
**Figure 3.5.** *Hydroelectric development gallery*



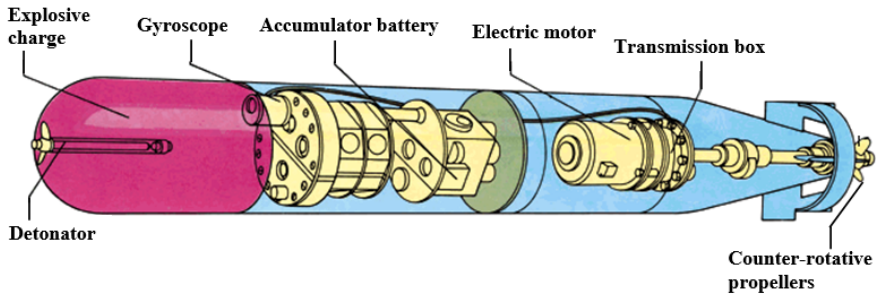
**Figure 3.6.** *Principle of operation of a gravity-powered hydroelectric power plant*



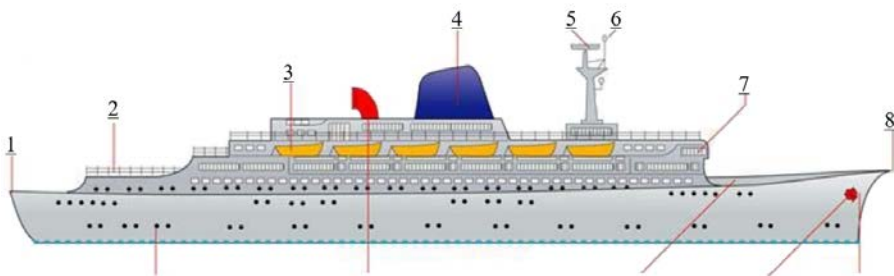
**Figure 3.7.** *Sliding a concrete block along the bottom of a river*



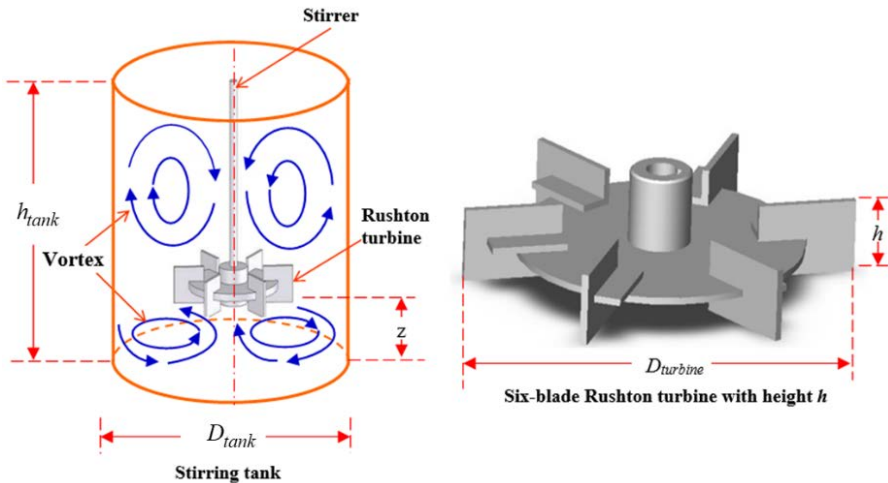
**Figure 3.8.** *The two main types of levees*



**Figure 3.13.** Example of a torpedo



**Figure 3.15.** Example of a ship designed for carrying passengers: 1) pump; 2) deck; 3) lifeboat; 4) chimney; 5) radar; 6) masthead light; 7) bridge; 8) bow; 9) anchor; 10) study; 11) bulwark; 12) windsock; 13) porthole



**Figure 3.16.** Stirring tank with six-blade Rushton turbine<sup>19</sup>



